

Determining the Relativistic Effects of Muons via a High-Altitude Experiment

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1. Background

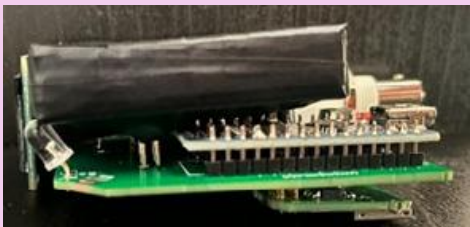
- ✿ According to the standard model, a muon is the second generation of charged lepton, and one of the six fundamental leptons featured in the model.
- ✿ Muons are encountered daily as the sun's cosmic rays collide with the atoms within the stratosphere to create pions, kaons, and muons.
- ✿ This experiment measures the count rate and decay patterns of muons, to inform interpretations related to special relativity.

2. Hypothesis to be tested

- ✿ Special relativity states that the laws of physics are the same for all observers relative to each other. Given the speed of light remains constant, time dilation is a product of special relativity.
- ✿ This explains how muons could be detected at altitudes where their lifetime should not allow.
- ✿ To a stationary observer, a muon travelling near the speed of light appears to experience time moving slower.
- ✿ Accordingly, muons can be detected at lower altitudes as a muon lifetime appears to be longer to an observer.

3. Apparatus

- ✿ A homemade muon detector



4. Methodology

- Step 1:** Power the detector through the Arduino nano and wait for two minutes for the count rate to even out.
- Step 2:** Record the count rate in 2 minute intervals.
- Step 3:** Eliminate the risk of a false readings from the connection between the SiPM PCB & the corresponding HV connector by completing a 'power off' interval.
- Step 4:** After the count rate drops as the plane descends, stop taking measurements.

5. Critical formulae

Gamma Factor

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \frac{1}{\sqrt{1 - \beta^2}} = \frac{dt}{d\tau}$$

Time dilation

$$T = \frac{T_0}{\sqrt{1 - \frac{v^2}{c^2}}}$$

6. Conclusion

- ✿ The results in Figure 1 show an increased muon count (to ~21.5 - 22) as the airplane altitude increases.
- ✿ Taking v to be $0.99c$, we get $\gamma = 7.09$
- ✿ The graph in Figure 2 predicts the count rate of muons without taking the gamma factor into account.
- ✿ The graph in Figure 3 takes gamma into account to perform accurate predictions of count rate based on altitude.
- ✿ From this, we can conclude that time dilation allows us to observe muons at relatively low altitude, though some will decay before being detected at the surface.

7. Figures

Figure 1: Muon Count Rates at altitude

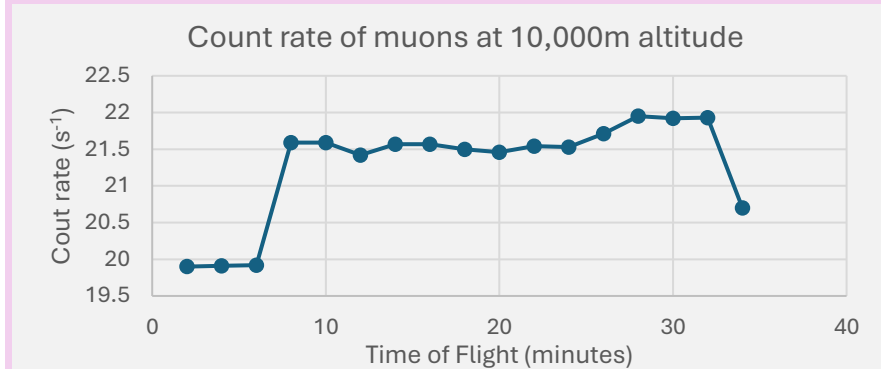


Figure 2:
Non-relativistic curve

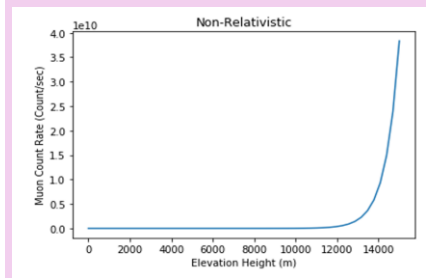
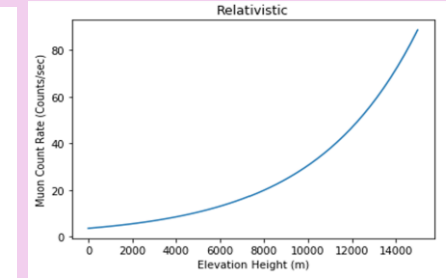


Figure 3:
Relativistic curve



8. References

- ✿ CosmicWatch, cosmicwatch.lns.mit.edu, 2017, accessed at: [CosmicWatch::catch yourself a muon](https://cosmicwatch.lns.mit.edu)
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